

HW 3

1. A particle moves along the x -axis so that its velocity v at time t , for $0 \leq t \leq 5$, is given by $v(t) = \ln(t^2 - 3t + 3)$.

- Find the acceleration of the particle at time $t = 4$.
- Is the particle speeding up or slowing down at $t = 4$? Explain.
- Find all times t in the open interval $0 < t < 5$ at which the particle changes direction. During which time intervals, for $0 \leq t \leq 5$, does the particle travel to the left?
- Find the average acceleration of the particle over the interval $0 \leq t \leq 2$.

A particle moves along the y -axis so that its velocity v at time $t \geq 0$ is given by $v(t) = 1 - \tan^{-1}(e^t)$. At time $t = 0$, the particle is at $y = -1$.

- Find the acceleration of the particle at time $t = 2$.
- Is the speed of the particle increasing or decreasing at time $t = 2$? Give a reason for your answer.
- Find the time $t \geq 0$ at which the particle reaches its highest point. Justify your answer.

A particle moves along the x -axis so that its velocity at any time t is given by $v(t) = -(t+1)\sin\left(\frac{t^2}{2}\right)$.

- Find the acceleration of the particle at $t = 2$. Is the speed of the particle increasing at $t = 2$? Why or why not?
- Find all times in the interval $0 \leq t \leq 3$ when the particle changes direction. Justify your answer.
- If the particle starts at the origin at $t = 0$, on which side of the origin will the particle be at $t = 2$? Justify your answer.

A particle moves along the x -axis so that its velocity at any time t , for $0 \leq t \leq 16$, is given by $v(t) = e^{2\sin t} - 1$. At time $t = 0$, the particle is at the origin.

- At what time is the particle at rest? Justify your answer.
- During what intervals of time is the particle moving to the left? Give a reason for your answer.
- What is the acceleration of the particle at time $t = 2$? Is the particle's speed increasing or decreasing at time $t = 2$? Justify your answer.

An object moves along the x -axis with initial position $x(0) = 2$. The velocity of the object at time $t \geq 0$ is given

$$\text{by } v(t) = \sin\left(\frac{\pi}{3}t\right).$$

- What is the acceleration of the object at time $t = 4$?
- Consider the following two statements.

Statement I: For $3 < t < 4.5$, the velocity of the object is decreasing.

Statement II: For $3 < t < 4.5$, the speed of the object is increasing.

Are either or both of these statements correct? For each statement provide a reason why it is correct or not correct.

A particle moves along the x-axis in such a way that its position at time t for $t \geq 0$ is given by

$$p(t) = \frac{1}{3}t^3 - 3t^2 + 8t.$$

- Show that at time $t = 0$ the particle is moving to the right.
- Find all values of t for which the particle is moving to the left.
- What is the position of the particle at time $t = 3$?
- When $t = 3$, what is the total distance the particle has traveled?

2.

A particle moves on the x-axis in such a way that its position at time t is given by

$$p(t) = (2t-1)(t-1)^2.$$

- At what times t is the particle at rest? Justify your answer.
- During what interval of time is the particle moving to the left? Justify your answer.
- At what time during the interval found in (b) is the particle moving most rapidly (that is, the speed is a maximum)? Justify your answer.

3.

A particle moves along the x-axis so that at time t its position is given by $p(t) = t^3 - 6t^2 + 9t + 11$.

- What is the velocity of the particle at $t = 0$?
- During what time intervals is the particle moving to the left?
- What is the total distance traveled by the particle from $t = 0$ to $t = 2$?
- For what values of t is the speed increasing?

4.

A particle starts at time $t = 0$ and moves on a number line so that its position at time t is given by

$$p(t) = (t-2)^3(t-6).$$

- When is the particle moving to the right?
- When is the particle at rest?
- When does the particle change direction?
- What is the farthest to the left of the origin that the particle moves?